

**Seventh Semester B.E. Degree Examination, June-July 2009**  
**Fuzzy Logic Control**

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions.

- 1 a. Explain the following with example:  
 i) Normal fuzzy set  
 ii) Convex fuzzy set  
 iii)  $\alpha$ -cut  
 iv) Level set. (10 Marks)
- b. Let  $X = \{x_1, x_2\}$ ;  $Y = \{y_1, y_2\}$ ;  $Z = \{z_1, z_2, z_3\}$  and if R represents the relation between X & Y and S represents the relation between Y and Z which are given as

$$R = \begin{matrix} & y_1 & y_2 \\ x_1 & \begin{bmatrix} 0.7 & 0.5 \end{bmatrix} \\ x_2 & \begin{bmatrix} 0.8 & 0.4 \end{bmatrix} \end{matrix} \quad S = \begin{matrix} & z_1 & z_2 & z_3 \\ y_1 & \begin{bmatrix} 0.9 & 0.6 & 0.2 \end{bmatrix} \\ y_2 & \begin{bmatrix} 0.1 & 0.7 & 0.5 \end{bmatrix} \end{matrix}$$

Find out  $T = R \circ S$  by max - min method and max-dot method. (10 Marks)

- 2 a. Write a short note on fuzzy equivalence and tolerance relations. (06 Marks)

- b. Let  $X = \{a,b,c\}$  &  $Y = \{1,2,3\}$  and A be the fuzzy relation between X and Y and is given by

$$A = \left\{ \frac{1}{(a,1)} + \frac{0.6}{(a,2)} + \frac{0.4}{(a,3)} + \frac{0.5}{(b,1)} + \frac{0.8}{(b,2)} + \frac{0.2}{(b,3)} + \frac{0.4}{(c,1)} + \frac{0.1}{(c,2)} + \frac{0.3}{(c,3)} \right\}$$

Find the projection of A on X and projection of A on Y. (08 Marks)

- c. Given two fuzzy sets  $\underline{A} = \left\{ \frac{1}{1} + \frac{0.5}{2} + \frac{0.65}{3} + \frac{0.85}{4} + \frac{1}{5} \right\}$        $\underline{B} = \left\{ \frac{0.2}{1} + \frac{0.5}{2} + \frac{0.9}{3} + \frac{0.5}{4} \right\}$

Find (i)  $\underline{A} \cup \underline{B}$       (ii)  $\overline{\underline{A}} \cup \underline{B}$       (iii)  $\underline{A} \cup \overline{\underline{B}}$       (iv)  $\underline{A} \cap \overline{\underline{B}}$  (06 Marks)

- 3 a. Let  $U = \{1, 2, 3, 4\}$  and  $V = \{1, 2\}$ . Define a fuzzy set A and U by  $(A \rightarrow 'x$  is small')

$$A = \frac{1}{1} + \frac{0.7}{2} + \frac{0.3}{3} + \frac{0.05}{4} \quad \text{Define a relation R between U and V by : } (R \rightarrow 'x \text{ is close to } y')$$

$$R = \frac{1}{(1,1)} + \frac{1}{(2,2)} + \frac{0.8}{(1,2)} + \frac{0.8}{(2,1)} + \frac{0.8}{(3,2)} + \frac{0.5}{(3,1)} + \frac{0.5}{(4,2)} + \frac{0.2}{(4,1)}$$

Use the compositional rule of inference to find the corresponding fuzzy set B defined on V ( $B \rightarrow 'y$  is small'). (12 Marks)

- b. What is a fuzzy proposition? With example, interpret the connectives AND and OR used in fuzzy propositions. (08 Marks)

- 4 a. What are linguistic variables? Explain their relevance in fuzzy logic control. (08 Marks)

- b. Suppose  $X = \{1, 2, 3, 4, 5\}$  and small is interpreted as  $\underline{\text{small}} = \frac{1}{1} + \frac{0.8}{2} + \frac{0.6}{3} + \frac{0.4}{4} + \frac{0.2}{5}$

$$\text{and large as } \underline{\text{large}} = \frac{0.2}{1} + \frac{0.4}{2} + \frac{0.6}{3} + \frac{0.8}{4} + \frac{1}{5} \quad \text{If R is the relation that represents "if$$

 $X$  is small then Y is large else y is not very large" Find R. (12 Marks)

- 5 a. What is scaling factor? Explain the heuristic method of selecting a scaling factor. (06 Marks)  
 b. With a block diagram explain the structure of FKBC. (08 Marks)  
 c. Explain the defuzzification procedure by (i) Centre of gravity (ii) Centre of sums method. (06 Marks)
- 6 Determine the defuzzifier output by centre of gravity, centre of sums, centre of largest area, first of maxima and middle of maxima defuzzification methods. (20 Marks)

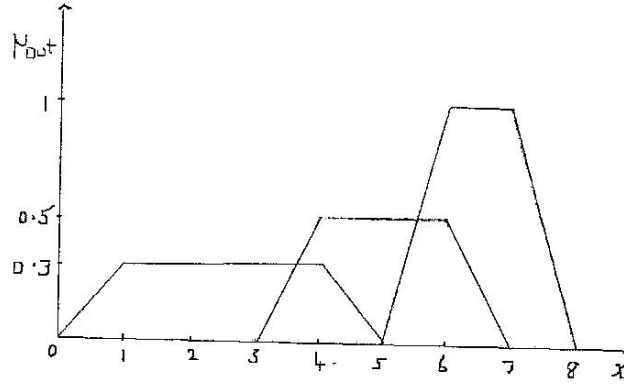


Fig.6

- 7 a. Show that FKBC is a non-linear transfer element of a system controller. (10 Marks)  
 b. Explain sliding mode FKBC. (10 Marks)
- 8 a. Explain any two adaptation techniques of a fuzzy system. (10 Marks)  
 b. Explain self organizing fuzzy controller. (10 Marks)

\*\*\*\*\*